## learn for later



Utrecht, August 19, 2022
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## what is mental math?

- OUT of your head (by heart)
- WITH your head


## what must?

OUT of your head:

-     + and - to 20
- time tables and their reverse
- home on the number line
- handy with zeros in multiplication
- lots of friends: the more, the better


## what more?

WITH your head:

- stringing + and - to 100 and 1000
- column wise + and -
- column wise $\times$ : one digit $\times$ two digit numbers
- division by multiplying up
- use of a calculator in time


## the smallest candy shop in the world



Stijn leaves the shop with 7 things for $€ 1$. what's in his bag?


## the candy



## smallest candy shop

- the smallest number of things you can buy is 4
- the biggest number of things you can buy is 20
- can you buy any number of things between 4 and 20?
- are you sure?
- can you prove it?


## some results of the lesson

## $15+15=30+25=55+10=65+5=70+15+15=E 1,00$

 48105B2 21| aantal dingen | 25 cent | 15 cent | 10 cent | 5 cent | samen 100 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | 4 | - | - | - | 100 |
| 5 | 3 | 1 | 1 | - | 100 |
| 6 | 3 | - | $2$ | 1 | 100 |
| 7 | $2$ | 1 | 3 | 1 | 100 |
| 8 |  | - | $4$ | $2$ | 100 |
| 9 | r | 4 | 3 | $1$ | 100 |
| 10 | - | - | 10 | - | 100 |
| 11 | - | - | $9$ | $2$ |  |
| 12 | - | - | $8$ | 4 |  |
| 13 | - | - | $7$ | 6 |  |
| 14 | $\sim$ | - | $6$ | $\delta$ |  |
| 15 | $\checkmark$ | - | $5$ | 10 |  |
| 16 | - | - | $4$ | 12 |  |
| 17 | - | $\sim$ | $3$ | 14 |  |
| 18 | $\checkmark$ | $\sim$ | $h$ | 16 |  |
| 19 | $\checkmark$ | - | 1 | $1-8$ |  |
| 20 | - | - | $\checkmark$ | $40$ |  |

## pieces of rope


a teacher needs, for a lesson, pieces of rope of 2.75 meter; she has a ball of rope of 80 meters.

- how many pieces can she get out of that?


## pieces of rope

- can you solve it?
- how?
- why is it so difficult?
- can children solve it?
- can grown ups solve it?


## reactions on the market

- french fries
- just a woman


## multiplying up



## starting problem

the teacher gets a new electric bicycle for his birthday. then he can go to school on that bike. a full battery is good for 90 kilometers.

- the teacher lives 6.25 kilometers from the school.
- how often can the teacher cycle back and forth to school before recharging the battery?
some results of the starting problem

90 km

$$
\begin{aligned}
& 1 x=6,25 \\
& 2 x=12,50 \\
& 4 x=25 \\
& 8 x=50 \\
& 12 x=75 \\
& 140 x=88,50
\end{aligned}
$$

$\frac{7 \times \text { Len en weer }}{14 \times \text { fen }}$

$$
\begin{gathered}
6,25\left(\begin{array}{l}
7 \\
\lg _{90} 0
\end{array} 12 \quad\right. \text { R.S. } \\
\frac{62,5}{175}-10 x \\
\frac{12,5}{5,0}-2 x
\end{gathered}
$$



$$
\begin{aligned}
& 12,5 / 80,10 \\
&-\frac{12,5}{77,5} \\
&-\frac{62,5}{1^{4} / 9^{10}} \\
&-\frac{12,5}{2,5}
\end{aligned}
$$



$$
7 R \cdot 2_{9} 5
$$

some results of the rope problem

$$
\begin{aligned}
& 10 \times 27,5 \\
& 20 \times 55 \\
& 30 \times 82,5 \\
& 29 \times 79,75
\end{aligned}
$$

2. 2 青

2; $75=1$
$27 . S=10$
渵

$$
S S, O=20
$$

$$
82,5=30
$$

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Some sides are much better than others!
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